

# NARCCAP UQ and Stat Stuff

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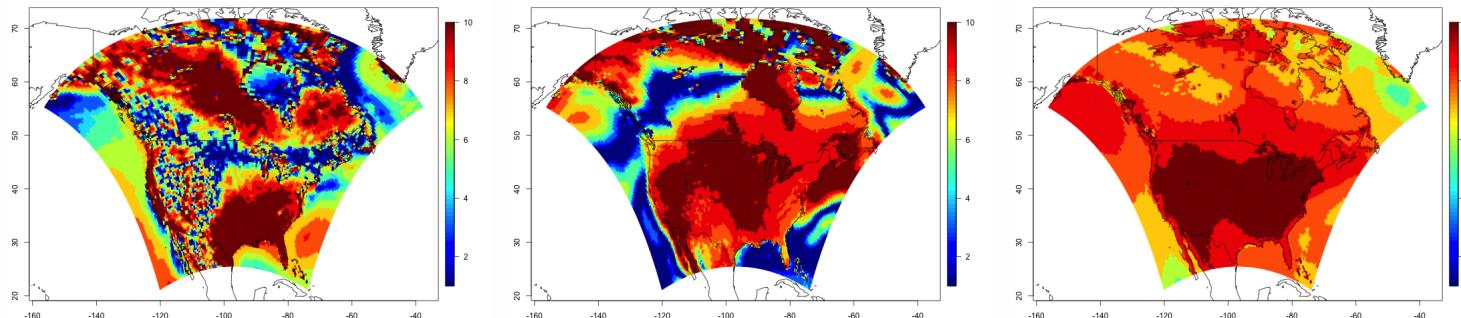
*Tammy Greasby, Matt Heaton (NCAR); Reinhard Furrer, Steve Geinitz (Zurich); Cari Kaufman (Berkeley); Dan Cooley , Grant Weller (CSU)*



*Supported by NSF DMS/ATM.*

# Outline and Goals

- Understanding sources of variation – functional ANOVA.
  - Implications for design of future experiments, “completing” the table, etc.
- Delivering climate change information and uncertainty – temperature profiles.
- Combining information and model weighting.
- Others – extremes, conveying uncertainty, stat methods, etc.

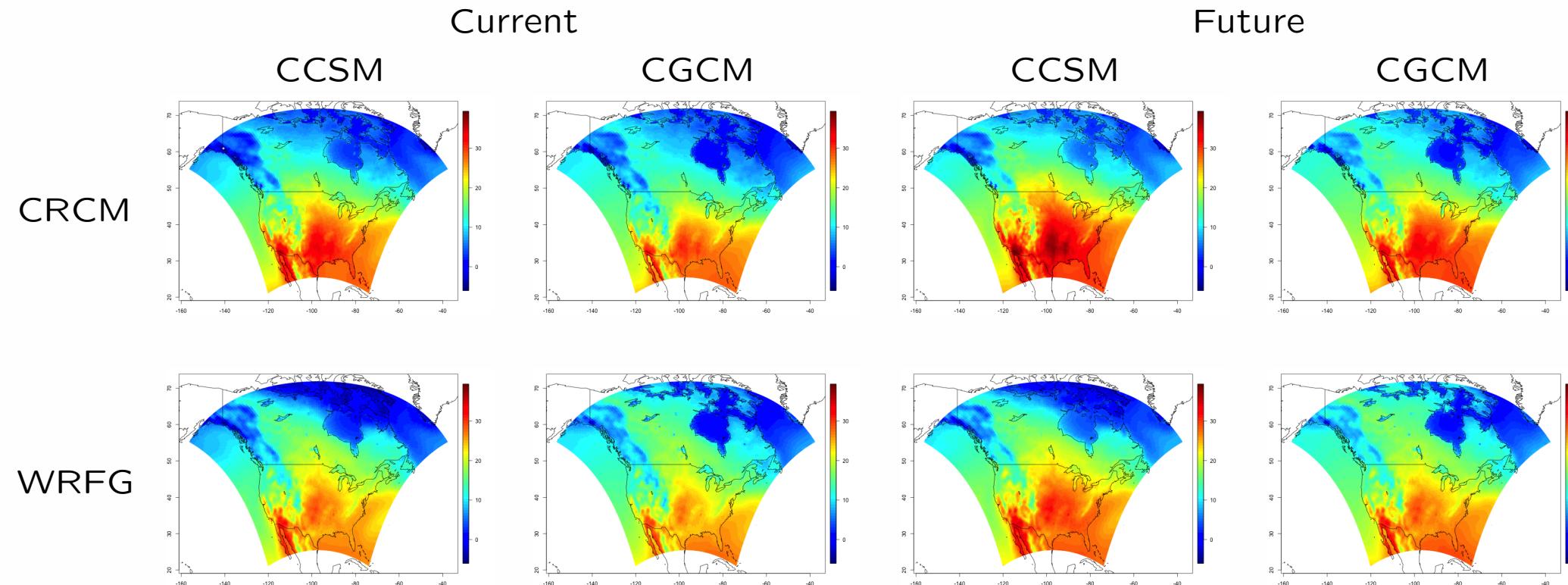


# The NARCCAP Design

	Phase I	Phase II			
	NCEP	GFDL	CGCM3	HADCM3	CCSM
CRCM	finished		finished		finished
ECP2	finished	finished		planned	
HRM3	finished	finished		finished	
MM5I	finished			running	finished
RCM3	finished	finished	finished		
WRFG	finished		finished		finished

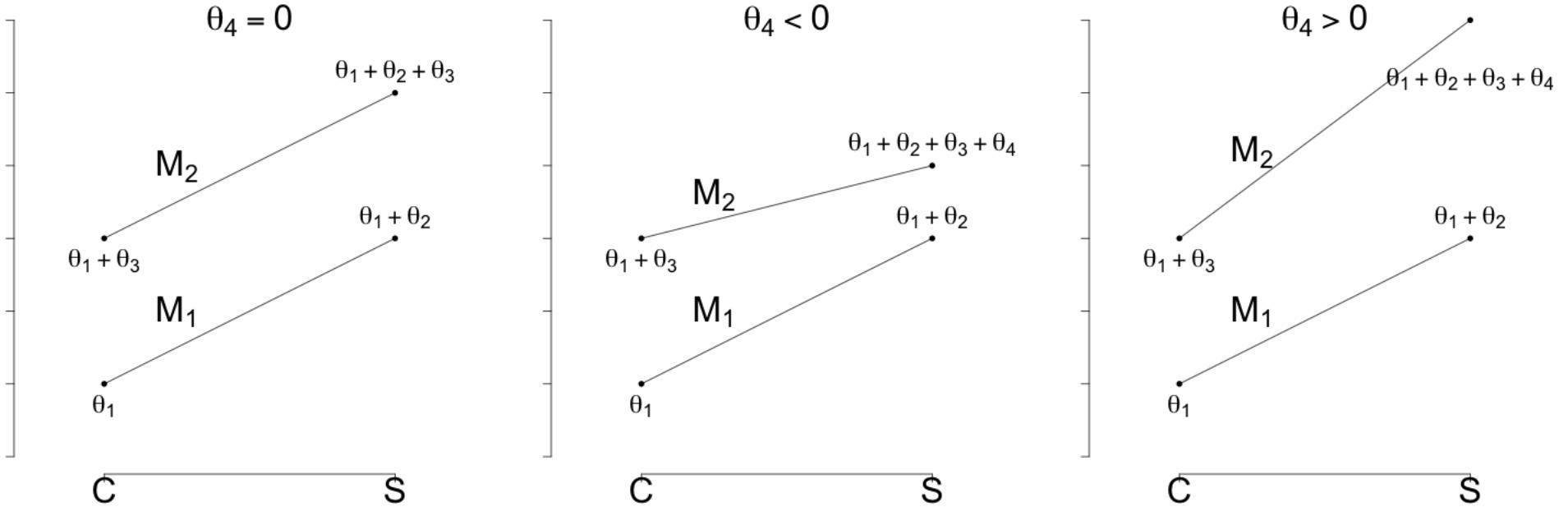
- Phase I: 1980-2000
- Phase II: 1971-2000 (Current), 2041-2070 (Future)
- All future runs use the A2 scenario
- Focus on seasonal summaries

# A $2^3$ example



30-year average summer (JJA) temperature.

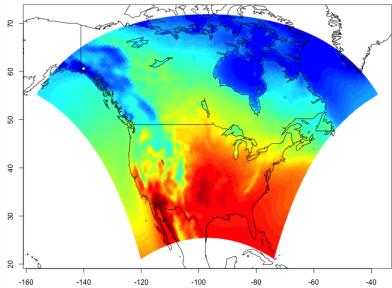
*Reinhard Furrer, Steve Geinitz (Zurich), Kari Kaufman (Berkeley)*



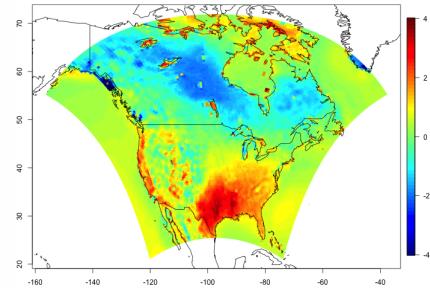
Does Model 2 respond to the forcing in the same way that Model 1 does ( $\theta_4 = 0$ )? Or does it respond in a way that is systematically different ( $\theta_4 \neq 0$ )?

# A $2^3$ example

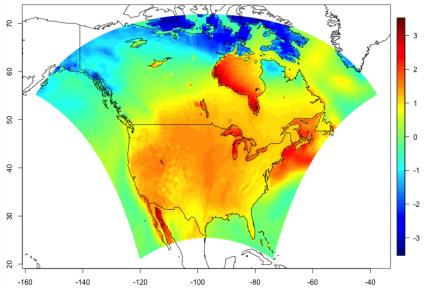
Baseline



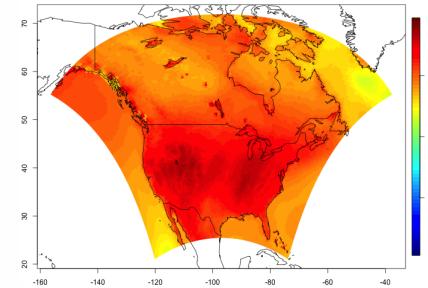
RCM



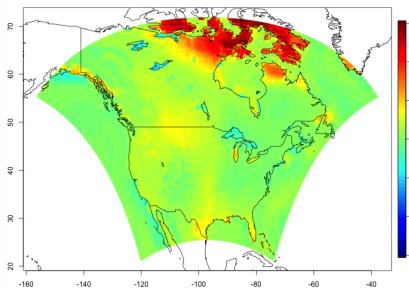
GCM



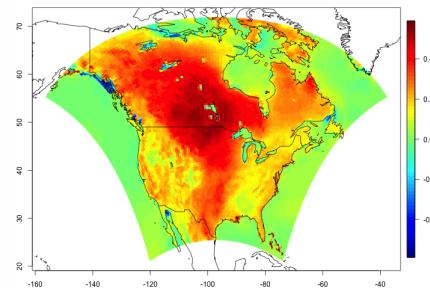
Scenario



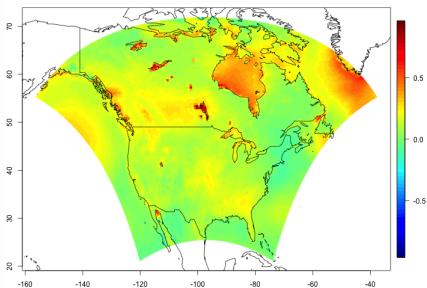
RCM\*GCM



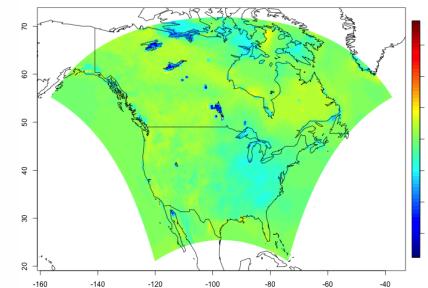
RCM\*Scenario



GCM\*Scenario



RCM\*GCM\*Scenario



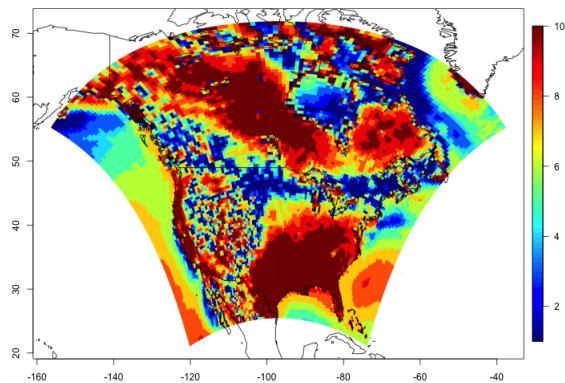
	DF	SS	MS	F	p-value	
GCM	1	5.51	5.51	2.01	0.16	
RCM	1	493.37	493.37	180.27	<2.2e-16	***
Scenario	1	387.73	387.73	141.67	< 2.2e-16	***
GCM:RCM	1	47.43	47.43	17.33	4.42e-05	***
GCM:Scenario	1	53.92	53.92	19.70	1.4e-05	***
RCM:Scenario	1	2.89	2.89	1.06	0.30	
GCM:RCM:Scenario	1	0.08	0.08	0.03	0.86	
Residuals	232	634.94	2.74			

An ANOVA table for a single grid near the S. Dakota, N. Dakota, Minnesota border.

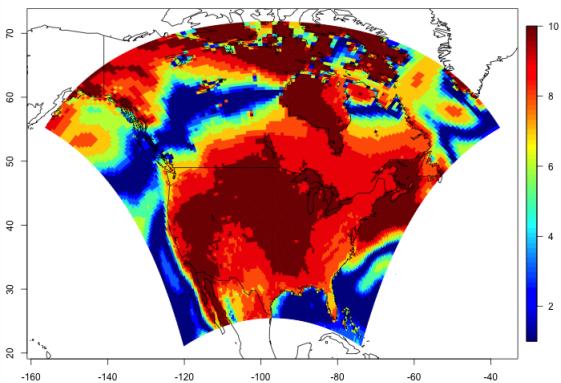
Interpretation complicated by spatial dependence, large numbers of tests, etc.

Issues can be addressed by treating the “effects” as spatial processes in a functional ANOVA framework embedded in a Bayesian hierarchical model.

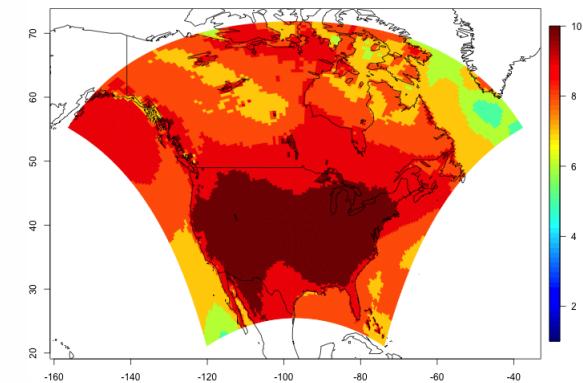
RCM



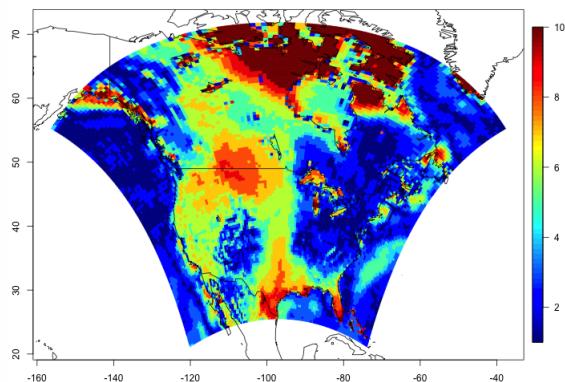
GCM



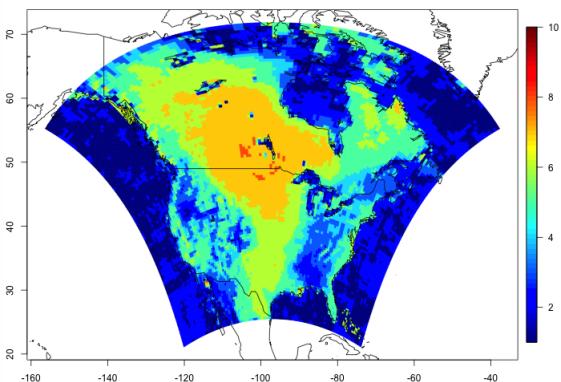
Scenario



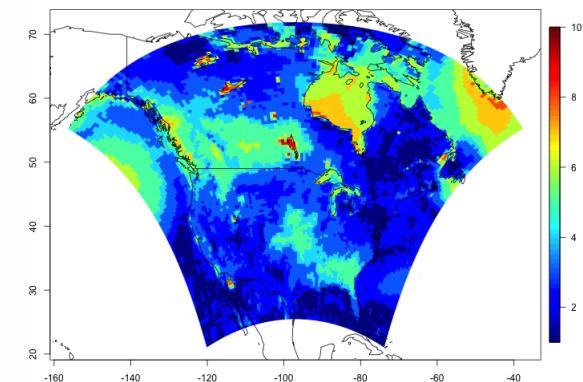
RCM★GCM



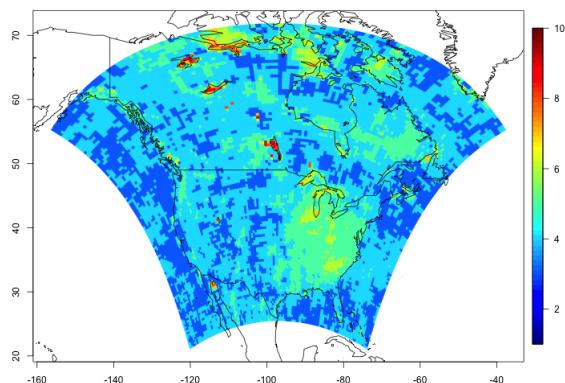
RCM★Scenario



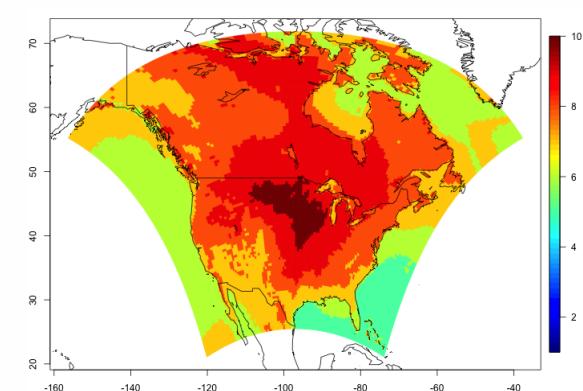
GCM★Scenario



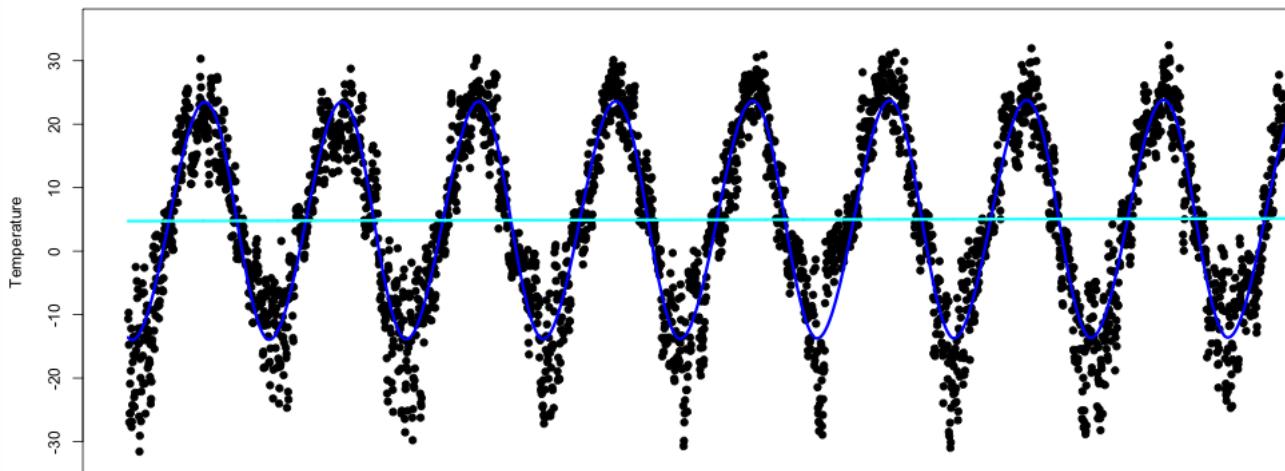
RCM★GCM★Scenario



Finite-sample variances  
via a Bayesian hierarchical  
spatial model



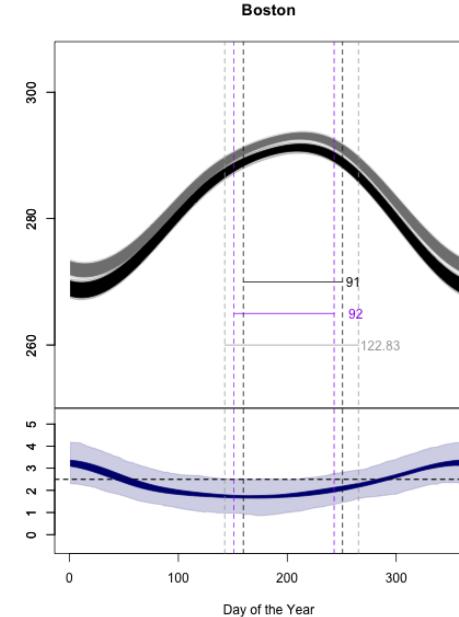
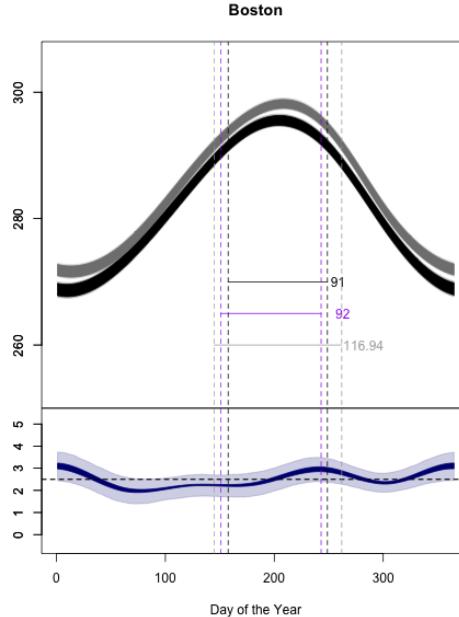
# Annual Temperature Profiles



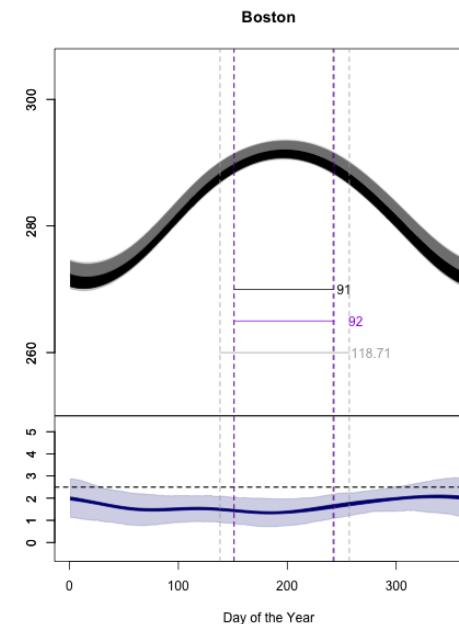
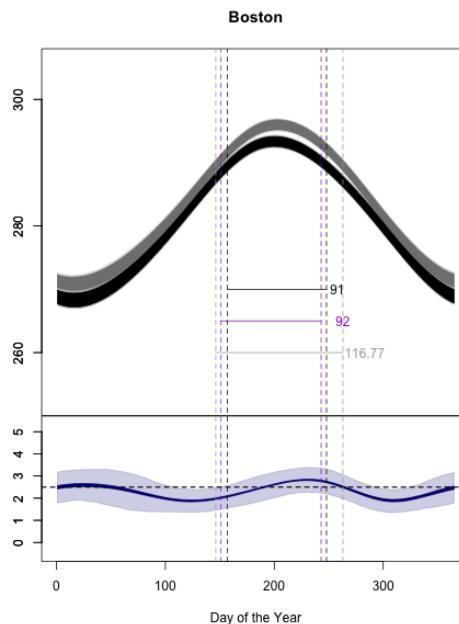
For each grid box, fit a periodic spline w/temporal trend to both current and future runs for a particular model. Allow coefficients to “borrow strength” through a multivariate spatial model on the coefficients of the spline.

*Tammy Greasby (NCAR)*

CCSM

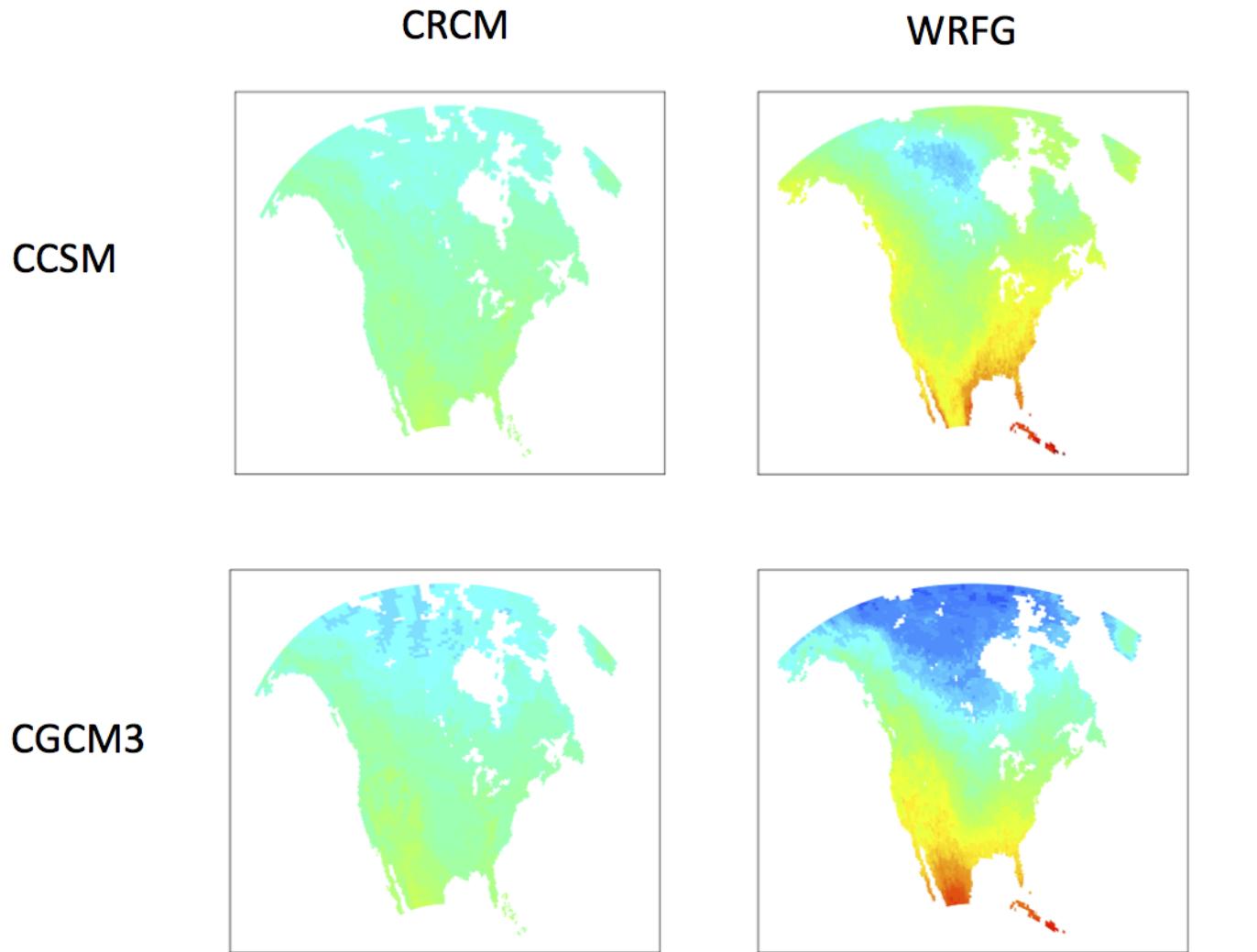


CGCM3

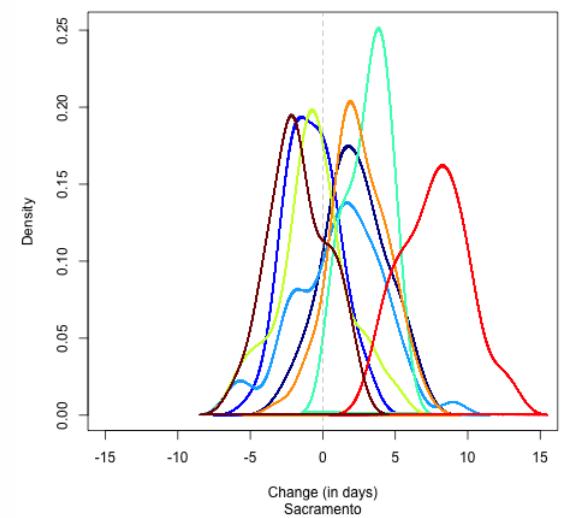
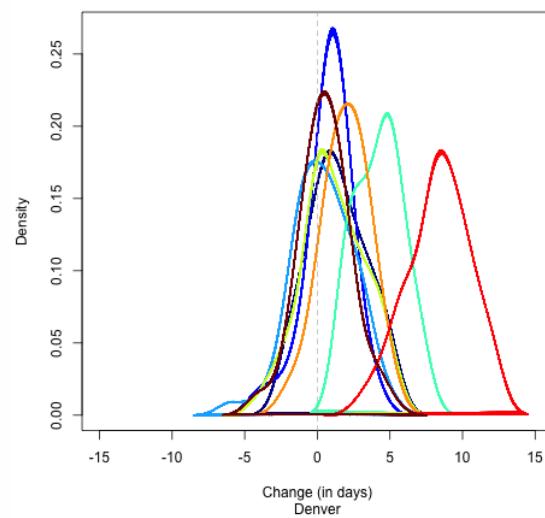
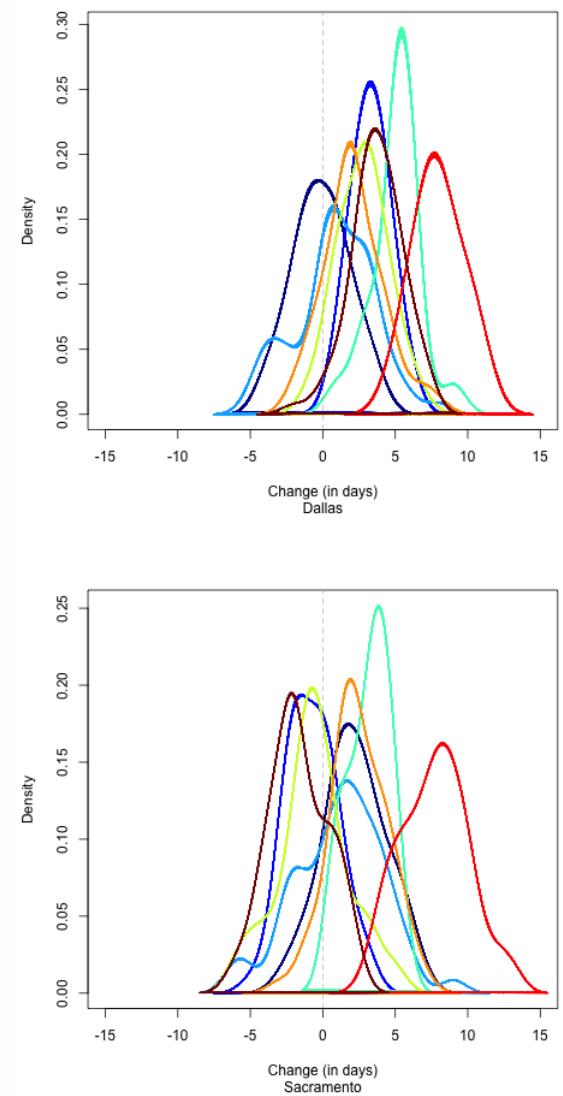
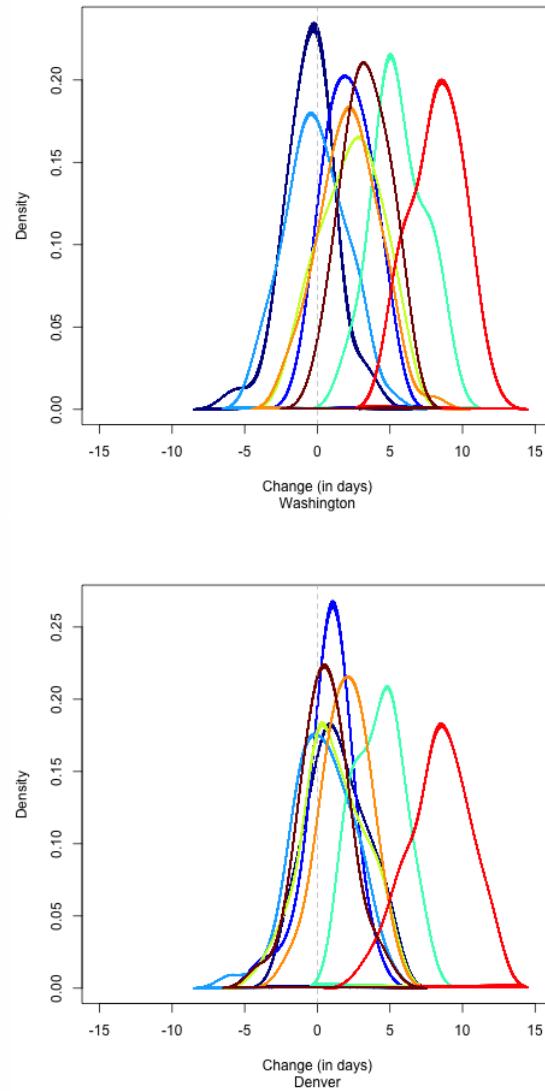
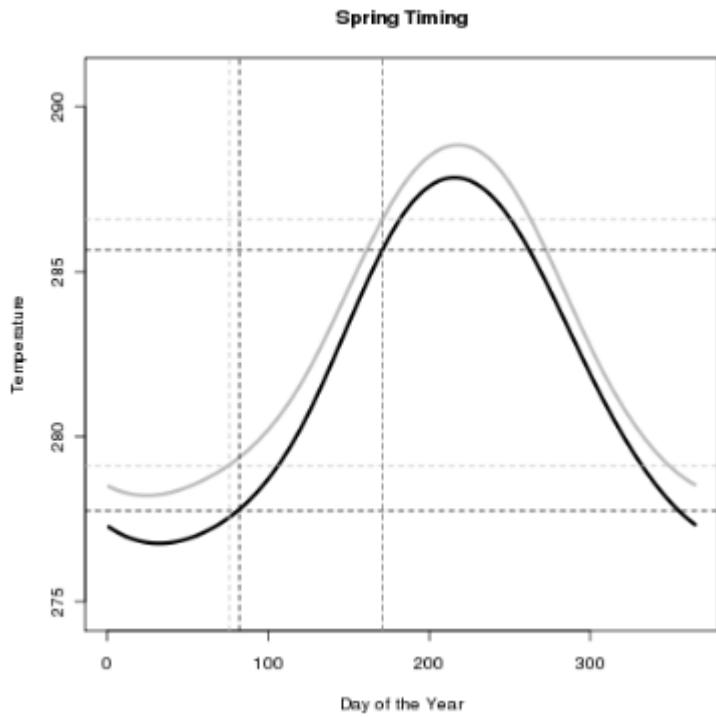


CRCM

WRFG



Posterior mean length of increase (days) in summer-like temperatures.  
Other measures (e.g., growing-degree days, heating/cooling-degree days, etc.) can also be examined.



Onset of spring-like temperatures.

# The Bayesian Paradigm

Postulate a model (pdf) for data that depends on some parameters:

$$Y_1, \dots, Y_n \sim \pi(Y_1, \dots, Y_n | \theta).$$

⇒ This forms the *likelihood*.

Postulate a model (pdf) for the parameters:

$$\theta \sim \pi(\theta)$$

⇒ This forms the *prior*.

Inference follows by examining of the posterior distribution:

$$\begin{aligned} \pi(\theta | Y_1, \dots, Y_n) &\propto \pi(Y_1, \dots, Y_n | \theta) \pi(\theta) \\ \text{posterior} &\propto \text{likelihood} \times \text{prior} \end{aligned}$$

⇒ From *Bayes' Theorem*.

# A Simple Model

$$Y_1, \dots, Y_n \sim \mathcal{N}(\mu, \sigma^2)$$

$$\begin{aligned}\mu|\sigma^2 &\sim \mathcal{N}(\mu_0, \sigma^2/\kappa_0) \\ \sigma^2 &\sim \text{Inv-}\chi^2(\nu_0, \sigma_0^2)\end{aligned}$$

Posterior distribution for  $\mu$ :

$$p(\mu|Y_1, \dots, Y_n) = t_{\nu_n}(\mu_n, \sigma_n^2, \kappa_n)$$

$$\begin{aligned}\mu_n &= \frac{\kappa_0}{\kappa_0 + n} \mu_0 + \frac{n}{\kappa_0 + n} \bar{Y} \\ \kappa_n &= \kappa_0 + n \\ \nu_n &= \nu_0 + n \\ \nu_n \sigma_n^2 &= \nu_0 \sigma_0^2 + (n - 1)s^2 + \frac{\kappa_0 n}{\kappa_0 + n} (\bar{Y} - \mu_0)^2\end{aligned}$$

# A Simple Model

$$Y_1, \dots, Y_n \sim \mathcal{N}(\mu, \sigma^2)$$

$$\begin{aligned}\mu|\sigma^2 &\sim \mathcal{N}(\mu_0, \sigma^2/\kappa_0) \\ \sigma^2 &\sim \text{Inv-}\chi^2(\nu_0, \sigma_0^2)\end{aligned}$$

Posterior predictive distribution:

1. Sample  $\sigma^2|\{Y_i\}$  from  $\text{Inv-}\chi^2(\nu_n, \sigma_n^2)$ .
2. Sample  $\mu|\sigma^2, \{Y_i\}$  from  $\mathcal{N}(\mu_n, \sigma^2/\kappa_n)$ .
3. Sample  $Y^*$  from  $\mathcal{N}(\mu, \sigma^2)$ .

# Model weighting

The Tebaldi model:

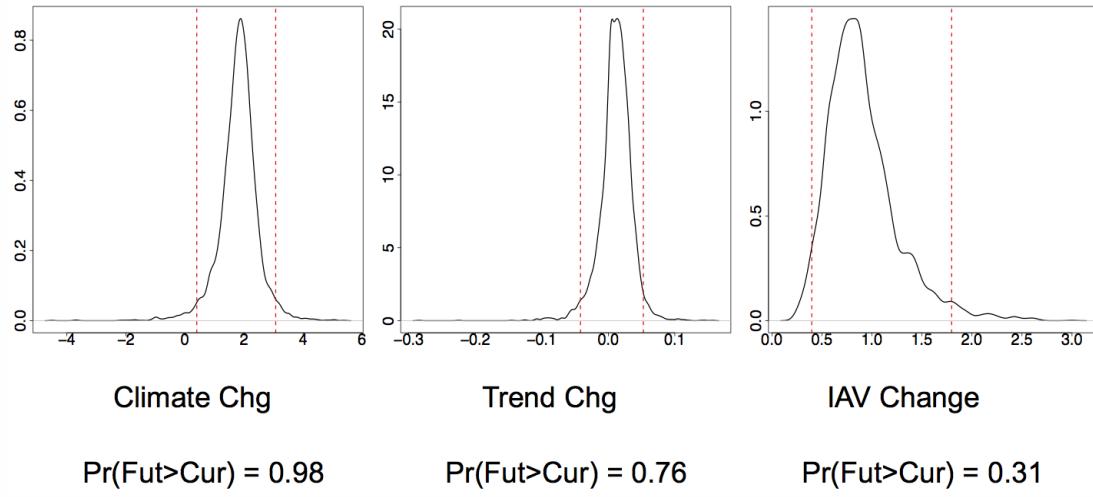
$$X_0 \sim \mathcal{N}(\mu, \lambda_0^{-1})$$

$$X_j \sim \mathcal{N}(\mu, \lambda_j^{-1})$$

$$Y_j \sim \mathcal{N}\left(\nu + \beta(X_j - \mu), (\theta\lambda_j)^{-1}\right)$$

- $X_0$  indicates an observed climate
- $X_j$  indicates model output for the current time period  $j = 1, \dots, 13$ .
- $Y_j$  indicates model output for the future time period.
- $\mu$  is current mean temperature,  $\nu$  is future temperature
- $\theta$  allows the climate model variance to change between time periods.
- $\beta$  accounts for correlation between the current and future climate models.  $\beta = 1$  is equivalent to modeling climate change directly.

- Modify Tebaldi model to:
  - Incorporate multiple observational datasets.
  - Model precisions ( $\lambda$ s), which control the influence of a particular model on estimates of  $\mu$ ,  $\nu$  and  $\nu - \mu$ , as a function of NARCCAP design (GCM, RCM, scenario).
  - *Tammy Greasby (NCAR)*
- Start from scratch (the kitchen sink model):
  - Incorporate multiple observational datasets.
  - Incorporate GCMs, NCEP-driven RCMs, GCM-driven RCMs.
  - Incorporate “familial” relationship between GCMs and RCMs.
  - Include model-to-model correlations and “bias” terms.
  - *Matt Heaton (NCAR)*

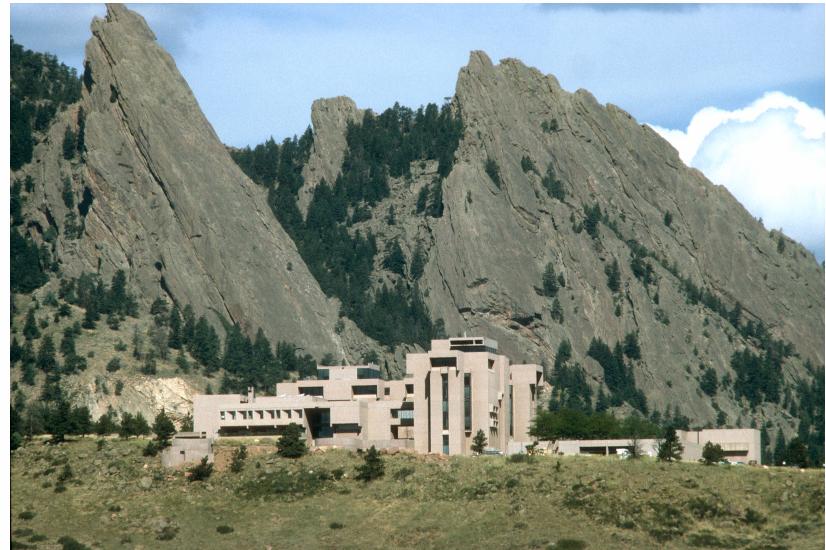


The Kitchen Sink Model:  
Pacific Southwest winter temperatures.

Data	Current Weight	Future Weight
UDEL	0.245	NA
CRU	0.224	NA
CRCM	0.006	NA
ECP2	0.020	NA
HRM3	0.045	NA
MM5I	0.021	NA
RCM3	-0.000	NA
WRFG	0.010	NA
CCSM	0.081	0.190
CGCM3	0.083	0.186
GFDL	0.066	0.127
HADCM3	0.084	0.204
CRCM-ccsm	0.013	0.066
CRCM-cgcm3	0.012	0.034
ECP2-gfdl	0.017	0.048
HRM3-hadcm3	0.025	0.052
MM5I-ccsm	0.013	0.021
RCM3-cgcm3	0.011	0.021
RCM3-gfdl	0.006	0.005
WRFG-ccsm	0.006	0.005
WRFG-cgcm3	0.014	0.050

# Questions?

Many opportunities for visits and collaboration: ASP, RSVP, SIParCs, GSP, IMAGe, Theme-of-the-Year,...



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*Thank You!*

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